

The following topics briefly summarize the mathematics minimums that you need to know for a general chemistry course.

POWERS AND ROOTS

$$a^n = a \cdot a \cdot \dots \cdot a \quad (n \text{ factors})$$

$$a^m a^n = a^{m+n}$$

$$(a^m)^n = a^{m \times n}$$

$$(ab)^n = ab \cdot ab \cdot \dots \cdot ab \quad (n \text{ factors}) = a^n b^n$$

$$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$$

$$(a^m b^n)^p = a^{m \times p} b^{n \times p}$$

$$\text{If } a \neq 0, \text{ then } a^{-n} = \frac{1}{a^n}$$

$$\frac{a^n}{a^m} = a^{n-m} \quad \text{if } n > m, \quad = \frac{1}{a^{m-n}} \quad \text{if } n < m, \quad = 1 \quad \text{if } n = m$$

If m and n are both integers with $n > 0$, and if $\sqrt[n]{a}$ exists, then

$$a^{1/n} = \sqrt[n]{a} \quad \text{and} \quad a^{m/n} = (\sqrt[n]{a})^m = \sqrt[n]{a^m}$$

$$\text{If } a \neq 0, \text{ then } a^0 = 1$$

ALGEBRA

The associative law of addition: $(a+b)+c = a+(b+c)$

The associative law of multiplication: $(ab)c = a(bc)$

The commutative law of addition: $a+b = b+a$

The commutative law of multiplication: $ab = ba$

The distributive law: $a(b+c) = ab+ac$

Additive inverse exists: $a+x=0, \quad x=-a$

Multiplicative Inverse of a is (if $a \neq 0$): $a \times \left(\frac{1}{a}\right) = 1$

Example: Multiplying by equivalent amounts on each side of an equation

$$AB = CD \Rightarrow \left(\frac{1}{B}\right)AB = \left(\frac{1}{B}\right)CD \Rightarrow A = \frac{CD}{B}$$

$$\frac{A}{B} = \frac{C}{D} \Rightarrow \frac{A}{B} \times B = \frac{C}{D} \times B \Rightarrow A = \frac{CB}{D}$$

CONVERSION FACTORS

Each of the conversion factors produces a new number in different units.

$$X \text{ unit } a \times \left(\frac{Y \text{ unit } b}{1 \text{ unit } a}\right) \times \left(\frac{Z \text{ unit } c}{1 \text{ unit } b}\right) = XYZ \text{ unit } c$$

LOGARITHMS

Base The number that is raised to the x power as in 10^x or e^x . For the logarithm to the base b this means:

$$\log_b b = 1$$

Inverse functions Logarithms are inverse functions for the base raised to a power.

$$\text{General: } y = b^x \Rightarrow \log_b y = \log_b b^x = x$$

$$\text{Base 10: } y = 10^x \Rightarrow \log_{10} y = \log_{10} 10^x = x$$

$$\text{Base } e: y = e^x \Rightarrow \ln y = \ln e^x = x$$

Facts and manipulations of logarithms:

$$\log_b 1 = \log_b b^0 = 0$$

$$\log_b X^n = n \log_b X$$

$$\log_b (XY) = \log_b X + \log_b Y$$

$$\log_b \left(\frac{X}{Y} \right) = \log_b (XY^{-1}) = \log_b X + \log_b Y^{-1} = \log_b X - \log_b Y$$

$$\log_b \sqrt[r]{X} = \log_b X^{-r} = \frac{1}{r} \log_b X$$

If a and b are two bases and if X is any positive number, then

$$\log_a X = \frac{\log_b X}{\log_b a}$$

Converting between different bases:

A number, y , can be expressed as a base, b , to a power x :

Generally, for converting between base a and base b :

$$y = b^x \quad \text{then}$$

$$\log_b y = \log_b b^x = x \log_b b = x \quad \text{and}$$

$$\log_a y = \log_a b^x = x \log_a b \quad \text{substituting for } x$$

$$\log_a y = (\log_b y) \log_a b \quad \text{or} \quad \log_b y = \frac{\log_a y}{\log_a b}$$

Specifically, converting between base 10 and e :

$$\text{for } b = \text{base } e \text{ and } a = \text{base } 10 \text{ one gets: } \quad y = e^x = \exp(x)$$

$$\text{Then: } \log_e y = \ln y = x \quad \text{and} \quad \log_{10} y = x \log_{10} e$$

$$\text{Substituting for } x: \quad \log_{10} y = (\ln y) \log_{10} e$$

$$\text{or} \quad \ln y = \frac{\log_{10} y}{\log_{10} e} = \frac{\log_{10} y}{0.43429} = 2.303 \times \log_{10} y$$

ROOTS OF EQUATIONS

Second order, or Quadratic equation,

$$ax^2 + bx + c = 0 \text{ has solutions: } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

FUNCTIONS

You should be familiar with the following functions:

polynomials, e^x , $\ln x$, $\log_{10} x$, $\cos x$, $\sin x$, $\tan x$

I suggest you make plots of these functions.